## BEM 103 Introduction to Finance - Homework 3

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7.1 Portfolio.



These curves tell us:

- the expected returns do not change with  $\rho$ ;
- when  $\rho = -1$ , there is a portfolio with zero risk;
- when  $\rho = 1$ , the  $E[r_P] \sim \sigma[r_P]$  curve is a line connecting points standing for A and B;
- for  $-1 < \rho < 1$ , the  $E[r_P] \sim \sigma[r_P]$  curve is always between those of  $\rho = \pm 1$ .

**7.2** CAPM.  $r_f = 5\%$ ,  $E[r_m] = 14\%$ ,  $\beta = 0.5$ . The expected return of this stock is

$$E[r] = r_f + \beta (E[r_m] - r_f) = 9.5\%$$

**7.5** Portfolio.  $\sigma[r_A] = 5\%$ ,  $\sigma[r_B] = 20\%$ ,  $\rho_{A,B} = 0.25$ ,  $r_f = 5\%$ . Let P be the portfolio with 25% A, 25% B and 50% risk free asset.

 $\sigma^2 \left[ r_P \right] = 25\%^2 \sigma^2 \left[ r_A \right] + 2 \cdot 25\%^2 \rho_{A,B} \sigma \left[ r_A \right] \sigma \left[ r_B \right] + 25\%^2 \sigma^2 \left[ r_B \right] + 50\%^2 \cdot 0 \approx 0.003 \,.$  So  $\sigma \left[ r_P \right] \approx 5.45\%$ .

**7.9** *A*, *B* & *C*.

- (1) Since we have  $E[r_A] < E[r_B] < E[r_C]$  and  $\sigma[r_A] < \sigma[r_B] < \sigma[r_C]$ , we can not say that one is definitely better than another. Different stocks could be recommended according to different tastes of return and risk.
- (2) We have 3 choices:
  - $\frac{1}{2}A + \frac{1}{2}B$ .

$$E[r_{A,B}] = (0.06 + 0.1)/2 = 8\%, \quad \sigma[r_{A,B}] = 0.5 \times 0.1 = 5\%;$$

•  $\frac{1}{2}A + \frac{1}{2}C$ .

$$E[r_{A,C}] = (0.06 + 0.2)/2 = 13\%, \quad \sigma[r_{A,C}] = 0.5 \times 0.375 = 18.75\%;$$

• 
$$\frac{1}{2}B + \frac{1}{2}C$$
.  $E[r_{B,C}] = (0.1 + 0.2)/2 = 15\%$ , and

$$\sigma[r_{B,C}] = \sqrt{0.5^2 \times 0.1^2 + 2 \times 0.5^2 \times 0.2 \times 0.1 \times 0.375 + 0.5^2 \times 0.375^2} = 20.35\%.$$

Since we also have  $E[r_{A,B}] < E[r_{A,C}] < E[r_{B,C}]$  and  $\sigma[r_{A,B}] < \sigma[r_{A,C}] < \sigma[r_{B,C}]$ , none of these portfolio could be eliminated.

## 7.10 EotW. The discount rate for the publishing division is

$$r_P = r_f + \beta_P(E[r_m] - r_f) = 5\% + 1 \times 10\% = 15\%,$$

and that of the entertainment division is

$$r_E = r_f + \beta_E(E[r_m] - r_f) = 5\% + 1.5 \times 10\% = 20\%,$$

and for the entire firm, it is

$$r_F = r_f + \beta_F(E[r_m] - r_f) = 5\% + 1.3 \times 10\% = 18\%.$$

- (1) Since any project's IRR is less than  $r_F$ , no project is acceptable from the view of the opportunity cost of capital for the entire company.
- (2) Again, any project's IRR is less than the discount rate of its corresponding division, no project should be accepted.
- **7.11** Misui.  $\beta_s = 1.15$ ,  $\beta_d = 0.3$ ,  $r_f = 6\%$  and  $E[r_m] r_f = 10\%$ .
  - (1) From CAPM, the discount rate should be

$$r = r_f + \beta_s \left( E\left[r_m\right] - r_f \right) = 6\% + 1.15 \times 10\% = 17.5\%.$$

(2) The ratios of the debt and equity in the entire firm is 20% and 80%, respectively. Thus the entire firm has  $\beta = 20\%\beta_d + 80\%\beta_s = 0.98$ . So the discount rate should be

$$r = r_f + \beta \left( E\left[r_m\right] - r_f \right) = 6\% + 0.98 \times 10\% = 15.8\%$$